

A-LEVEL Statistics

Statistics 1B – SS1B Mark scheme

6380 June 2015

Version/Stage: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available from aqa.org.uk

Copyright © 2015 AQA and its licensors. All rights reserved.

AQA retains the copyright on all its publications. However, registered schools/colleges for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to schools/colleges to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Μ	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
В	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
–x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
С	candidate
sf	significant figure(s)
dp	decimal place(s)

Key to mark scheme abbreviations

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

General Notes for SS1B

- GN1 There is no allowance for misreads (MR) or miscopies (MC) unless specifically stated in a question
- **GN2** In general, a correct answer (to accuracy required) without working scores full marks but an incorrect answer (or an answer not to required accuracy) scores no marks
- **GN3** Where percentage equivalent answers are permitted in a question, penalise by **one accuracy mark** at the first **correct** answer but only if no indication of percentage (eg %) is shown
- **GN4** In probability questions, do **not** award **accuracy** marks for answers in the form of a ratio or odds (eg 7/20 as 7:20 or 7:13)

Q	Solution	Marks	Total	Comments	
1 (a)	Mode = <u>10</u>	B1		CAO; ignore any reference to 9 unless stated as the/a mode	
	Median = <u>11</u>	B1		CAO; providing not based on shown incorrect working	
	UQ = 14 $LQ = 10$	B1		Either CAO; ignore notation Can be implied from IQR = 4 with no working or from IQR = 4 not from incorrect working	
	$IQR = \underline{4}$	B1	4	CAO	
Notes	1 If values are not identified, then assume that order of values is mode, median, IQR 2 Ordering of days $(1, 1, 2, 3, 3, 4, 5, 7, 9) \implies mode = 3$, median = 3, IOR = $6 - 1.5 = 4.5 \implies$ no marks				
(b)	Mean = <u>11.8</u>	B2		CAO $\left(\sum f = 35 \text{ and } \sum fx = 413\right)$	
	Mean = 11.7 to 11.9	(B1)	2	AWFW	
Notes	1 Using only x-values gives mean = $11.22 \Rightarrow B0$ 2 Using only f-values gives mean = $3.889 \Rightarrow B0$ 3 If, and only if, B0, then award M1 for seen attempt at \sum	$fx \div 35$ or	for seen at	ttempt at 413÷35	
		T ()			
		Total	6		

Q	Solution	Marks	Total	Comments
2				Accept percentage equivalent answers in (a)
(a)(i)				but see GN3
(a)(l)	$P(X < 90) = P\left(Z < \frac{90 - 91}{0.8}\right)$	M1		Standardising 90 with 91 and 0.8; allow $(91 - 90)$
	= P(Z < -1.25) = 1 - P(Z < -1.25)	m1		Correct area change Can be implied by a correct answer or by an answer < 0.5
	= (1 - 0.89435) = 0.105 to 0.106	A1	(3)	AWFW (0.10565)
(ii)	$P(X \neq 90) = 1 \text{ or one or unity or } 100\%$	B1	(1)	CAO; accept nothing else but ignore zeros after decimal point (eg 1.00) Ignore additional words providing that they are not contradictory (eg certain so = 1)
Note	1 $P(X \neq 90) = P(Z \neq 0) \implies B0$ unless followed by 1 OE			
(iii)	P(91 < X < 92.5) = P(0 < Z < 1.875)			
	or = $(0.969 \text{ to } 0.972) - 0.5$ = $0.5 - (0.028 \text{ to } 0.031)$	B1		AWFW/CAO OE; can be implied by a correct final answer CAO/AWFW
	= <u>0.47</u>	B1	(2)	AWRT (0.46960)
			6	
(b)	$1\%(0.01) \implies z = -2.33 \text{ to } -2.32$	B1		AWFW; seen anywhere, ignore sign (-2.3263)
	$P(Y < 150) = P\left(Z < \frac{150 - 153}{\sigma}\right)$	M1		Standardising 150 with 153 and σ/s ; allow (153 – 150)
	$\frac{\pm (150 - 153)}{\sigma} = \begin{pmatrix} \pm 1.28 \text{ AWRT} \\ \text{or} \\ \pm 2.32 \text{ to } \pm 2.33 \text{ AWFW} \end{pmatrix}$	ml		(-1.2816) Can be implied by a correct answer (-2.3263)
	σ = <u>1.3</u>	A1	4	AWRT (1.28960)
Note	1 Award A0 if the signs are not consistent throughout, so, for	or example,	(150 - 153)/+2.3263 gives $\sigma = 1.3 \implies B1, M1, m1, A0$
		Total	10	

Q	Solution	Marks	Total	Comments
3 (a)(i)	r = 0.748r = 0.74 to 0.76r = 0.7 to 0.8	B3 (B2) (B1)		AWRT (0.74802) AWFW AWFW
	Attempt at $\sum x \sum x^2 \sum y \sum y^2 \& \sum xy$			364 10916 406 13688 & 11803 (all 5 attempted)
	or	(M1)		1452 1014 8 1245
	Attempt at S_{xx} S_{yy} & S_{xy} Attempt at substitution into correct			(all 3 attempted)
	corresponding formula for r r = 0.748	(m1) (A1)		AWRT
(ii)			3	
(11)	Moderate/(fairly/quite) strong positive (linear) correlation	Bdep1		Dependent on $0.7 \le r \le 0.8$ OE; must qualify strength and state positive
	marks on (the two) papers	B1	2	OE; providing $-1 < r < +1$
Notes	 Only accept phrases stated; ignore additional comments ur Use of: "very/extremely/relatively strong or high or big Accept "relationship/association/link" but not "trend" in: Do not accept "between papers" without further reference 	lless contract or good of stead of "co to marks	lictory r some or porrelation"	medium or average" \Rightarrow Bdep0
(b) (i)	Group U: $r = \frac{34.57}{\sqrt{279.71 \times 112.86}}$	M1		Correct numerical form; can be implied by a correct answer
	= 0.19 to 0.2	A1	2	AWFW (0.19457)
(ii)	Group T			
	Some/(fairly/quite/very) weak/little/slight/ (almost) no/hardly any (positive) correlation	B1		OE; must qualify stren gth
	<u>Group U</u> Some/(fairly/quite/very) weak/little/slight/ (almost) no/hardly any (positive) correlation	Bdep1	2	Dependent on $0.19 \le r_U \le 0.2$ OE; must qualify strength
Notes	1 Only accept phrases listed; ignore additional comments un 2 Use of: "low or small or poor or bad or unlikely or r 3 Accept "relationship/association/link" but not "trend" in: 4 "For each group" \Rightarrow B1 Bdep1 5 "For both gr	less contrad elatively" stead of "co oups" \Rightarrow	ictory ⇒ B0 prrelation" Bdep2	6 "No reference to groups (OE)" \Rightarrow B0
SC	1 "Correlation in (a)(ii) is spurious (OE)" \Rightarrow B1	* 1	<u>,</u>	
(iii)	(Both mean) marks for Group T are (much) larger than those for Group U	B1		OE
	extra tuition appears beneficial/effective	Bdep1	2	OE; dependent on B1
SC	1 "Group T candidates may have been more motivated so wo	uld have pe	rformed bet	ter even without extra tuition (OE)" \Rightarrow B0 B1
		Total	11	

Q	Solution	Marks	Total	Comments
4				Accept percentage equivalent answers in
(a)(i)				
	M M' Total	B1		0.12; CAO
	<i>E</i> 0.16 0.12 0.28	DI		
	<i>E'</i> 0.24 0.48 0.72	B1		0.4(0) and 0.72; CAO
	Total 0.40 0.60 1.00	B1		0.24 and 0.48; CAO
			3	
(ii)	$\mathbf{P}(\mathbf{D}_{1},\ldots,\mathbf{d}_{k-1})$			
	$P(\text{Buys exactly 1}) = 0.12 + [0.24 \text{ or } P(E' \cap M) \text{ from (i)}]$	M1		
	0.12 + [0.24 of 1(E + M) from (f)]	1011		
	= <u>0.36</u>	A1		CAO
(***)			2	
(111)	$\mathbf{P}(M \cap E) = 0.16$			
	$r(M \cap E) = 0.10$ which is	B2		Correct comparison of 0.16 with 0
	greater than/not equal to 0			L L
	or			
	$P(M \cup E) = 1 - 0.48 = 0.52$			
	but	(B2)		Correct comparison of 0.52 with 0.68
	P(M) + P(E) = 0.40 + 0.28 = 0.68		2	
			2	
	Part (a)	Total	7	

Q	Solution	Marks	Total	Comments
4	Continued	T ()	_	
	Part (a)	Total	7	Accent percentage equivalent answers in
				(b) & (c)(ii) but see GN3
(b)	SS'TotalT0.17000.11250.2825T'0.68000.03750.7175Total0.85000.15001.0000			(No marks for this table; it is simply here to help marking)
(i)	$P(4 \text{ papers}) = P(M \cap E \cap S \cap T) =$			
	$0.16 \times (0.85 \times 0.20)$ or 0.16×0.17	M1		All correct Can be implied by a correct answer
	= <u>0.027</u>	A1	2	AWRT (0.0272)
(ii)	$P(0 \text{ papers}) = P(M' \cap E' \cap S' \cap T') =$			
	$0.48 \times (0.15 \times 0.25)$ or 0.48×0.0375	M1		Seen Can be implied by a correct answer
	= <u>0.018</u>	A1	2	CAO (0.018)
(c) (i)	Chris (only) buys a Friday morning (newspaper) and a Saturday (morning) newspaper	B1 B1	2	Ignore additional comments about what he also does not buy
SCs	1 "Chris does not buy either a Friday evening or a Sunday (morning) newspaper" (OE) ⇒ B1 2 Statements of the form "(Friday morning) × (Saturday morning)" (OE) ⇒ B1 3 Statements involving "probability and/or intersection" ⇒ B1 max			
(ii)	$P(M \cap E' \cap S \cap T') =$			
	$0.24 \times (0.85 \times 0.80)$ or 0.24×0.68	M1		Seen Can be implied by a correct answer
	= <u>0.163</u>	A1	2	AWRT (0.1632)
Note	1 $(0.40 \times 0.72 \times 0.85 \times 0.80) = 0.19584 \implies M0 A0$			· · · · · · · · · · · · · · · · · · ·
		Total	15	

5 (a)Scatter diagram4 or 3 points correctB1(within tolerances on templat(b) (i) b (gradient/slope) = $\underline{10.0}$ b (gradient/slope) = $\underline{9.75}$ to 10.25 B2 (B1)AWRT AWFW	e)
(b) (i) $b (\text{gradient/slope}) = \underline{10.0}$ B2 AWRT ($b (\text{gradient/slope}) = \underline{9.75 \text{ to } 10.25}$ (B1) AWFW	
	10.00503)
$a \text{ (intercept)} = \frac{67.6 \text{ to } 67.7}{50 \text{ to } 90} B2 $ $a \text{ (intercept)} = \frac{50 \text{ to } 90}{50 \text{ to } 90} (B1) $ $AWFW $ $(AWFW)$	67.65292)
Attempt at $\sum x \sum x^2 \sum y \& \sum xy$ 690 49598 7580 & 5429 (all 4 attempted) ($\sum y^2 =$	10 5995000)
or (M1)	
Attempt at S_{xx} & S_{xy} 1988 & 19890 (both attempted)(S_{yy} =	= 249360)
Attempt at substitution into correct (m1)	
$b = 10.0$ (AWRT) $a = 67.6$ to 67.7 (AWFW) (A1 A1) $(\overline{x} = 69 \& (\overline{x} = 69 \& \overline{x}))$	$\overline{y} = 758$
(4)	
 3 Award 4 marks for y = (67.6 to 67.7) + 10x or for (67.6 to 67.7) + 10x 4 Values of a and b interchanged and equation y = ax + b used for drawing line ⇒ max of 4 marks 5 Values of a and b interchanged and equation y = a + bx used for drawing line ⇒ 0 marks 6 Values are not identified or simply b/a = # and a/b = #, then 9.75 to 10.25 ⇒ B1 and 50 to 90 ⇒ B1 but acc for example, as identification, [b = #, a = # with y = a + bx but no substitution for b & a] or [slope/gradient(b) = #, intercept(a) = #] 7 Answers in fractions can score at most M1 m1 8 Some/all of marks can be scored in (b)(ii), (b)(iii) & (c), even if some/all of marks are lost in (b)(i), but marks lost in (b be recouped by subsequent working in (b)(ii), (b)(iii) or (c) 	ept,)(i) cannot
Scatter diagram line correct B2 Within tolerance on template from $x = 50$ to $x = 80$ (2)	at least
Notes 1 If, and only if, B0, then award M1 for seen correct use of an equation for at least two points in range $x = 35$ to $x = 2$. If and only if, B0, then award M0 for points or line marked on scatter diagram without supportive working	100
2 II, and omy II, Bo, unch award who for points of the marked on scatter diagram without supportive working 6	
(ii) b: each/every customer generates on average £10 in takings B1 BF1 F on b providing $9.75 \le b$:	≤ 10.25
 Notes 1 To score any marks, an explanation must indicate change in x affecting change in y, not change in y affecting change in 2 As x increases then y increases by 10 (OE; context not required) ⇒ B1 BF0 3 Reference only to correlation ⇒ B0 BF0 	x
(iii) <i>a</i> : takings when no customers cannot be > 0 or when $x = 0$ then $y = 0$ or never no customers/x never $0/x$ always > 0 or $x = 0$ is outside range/extrapolation B 1 D E 1	
(c) $y(50) = \underline{\text{\pounds570}}$ B1 CAO; \pounds not required From calculation/graph/guess	(£567.90) swork
Total 11	

Q	Solution	Marks	Total	Comments
6	Accept 3 dp rounding of probabilities from tables in (b)			Accept percentage equivalent answers in (a) \Re (b) but see CN3
(a)	Use of B(24, 0.22) or B(40, 0.45)	M1		Indicated by an expression or by any one correct probability in (a) or (b)
	$P(C=2) = {\binom{24}{2}} (0.22)^2 (0.78)^{22}$	M1		Fully correct expression Can be implied by a correct answer Ignore extra terms
	= 0.056 to 0.057	A1	3	AWFW (0.05647)
(b) (i)	P(DC < 20) = 0.684 to 0.685	B1	(1)	AWFW (0.6844)
(ii)		7.54		
	P(DC > 15) = 1 - (0.2142 or 0.1326)	M1		Requires '1 $-$ (either value)'
	= <u>0.785 to 0.786</u>	A1	(2)	AWFW (0.7858)
Note	1 For stated answers: award B2 for 0.785 to 0.786 (AWFW	/); B1 for	0.867 to 0.8	368 (AWFW)
(iii)	$P(12 \le DC \le 24) = 0.9804 \text{ or } 0.9595 (p_1)$	M1		Can be implied by a correct answer
	MINUS 0.0179 or 0.0386 (<i>p</i> ₂)	M1		Can be implied by a correct answer
	= 0.96 to 0.963	A1	(3)	AWFW (0.9625)
Notes	1 First M1 is for $(+p_1)$ in a subtraction 2 Second M1 is for $(-p_2)$ in a subtraction 4 For stated answers: award B3 for 0.96 to 0.963 (AWFW)); B2 for 0	.94 (AWRT	3 $(1-p_2) - (1-p_1) \Rightarrow M1 M1 (A1)$ (A); B1 for 0.92 (AWRT)
			6	
(c)	p = 1 - 0.22 - 0.45 = 0.33	B1		CAO; can be implied
	Mean $(\mu \text{ or } \overline{x}) = 200 \times 0.33 = \underline{66}$	B1		CAO
	Variance $(\sigma^2 \text{ or } s^2) = 200 \times 0.33 \times 0.67$			
	= <u>44 to 44.3</u>	B1	3	AWFW (44.22)
Notes	1 If answers are not identified, then assume that order of values is (p) , mean, variance 2 When 44 to 44 3 is labelled as Sd(σ or s) \rightarrow B0			
SC	1 If mean is calculated from 200p with $p \neq 0.33$ but 0			
		Total	12	

Q	Solution	Marks	Total	Comments
7 (a)	Sd of \overline{A} = <u>0.43/$\sqrt{10}$ or 0.135 to 0.137</u> or Var of \overline{A} = <u>0.43²/10 or 0.0184 to 0.0186</u>	B1		CAO/AWFW(0.13598)Can be implied in what followsCAO/AWFW(0.01849)
	$P(\overline{A} > 1.25) = P\left(Z > \frac{1.25 - 1.16}{0.43/\sqrt{10}}\right)$	M1		Standardising 1.25 with 1.16 and (0.43/ $\sqrt{10}$) OE; allow (1.16 – 1.25)
	= P(Z > 0.6619) = 1 - P(Z < 0.6619)	m1		Correct area change Can be implied by a correct answer or by an answer < 0.5
	$= 1 - 0.74597 \qquad = 0.253 \text{ to } 0.255$	A1	4	AWFW (0.25403)
(b) (i)	<u>or</u> 96% (0.96) $\Rightarrow z = 2.05 \text{ to } 2.06$ $\Rightarrow t = 2.12 \text{ to } 2.13$	B1		AWFW(2.0537)AWFW(2.1247)
	CI for μ is $0.86 \pm \begin{pmatrix} 2.05 \text{ to } 2.06 \\ 2.12 \text{ to } 2.13 \\ 1.75 \text{ or } 1.80 \end{pmatrix} \times \frac{(0.65 \text{ to } 0.66)}{\sqrt{40 \text{ or } 39}}$	M2,1 (-1 ee)		Ignore any notation (1.75 & 1.80) are AWRT $0.65 \times \sqrt{\frac{40}{39}} = 0.65828$ No $\sqrt{n} \Rightarrow M0$
	Hence $0.86 \pm (0.21 \text{ to } 0.23)$ or $(0.63 \text{ to } 0.65, 1.07 \text{ to } 1.09)$	Adep1	4	CAO ± AWFW Dependent on award of M2 AWFW
Notes	 An incorrect expression for CI followed by a numerically c Evaluation of only one CL ⇒ (B1) M0 Adep0 Accept answers in grams 	orrect CI =	⇒ 2 solutio	ns \Rightarrow ((0 or 1) + 4)/2 \Rightarrow 2 marks
(ii)	Clear correct comparison of 1.16 with CI eg 1.16 is above CI or UCL < 1.16	BF1		F on CI providing it does not contain 1.16 Must have found an interval in (i) but quoting values for CI or CLs is not required
	Agree with claim or accept claim or Weight of apples is (likely to be) greater than that of pears	Bdep1	2	OE; dependent on BF1
Notes	 Statement must clearly indicate that "1.16 is above/outside/not within the CI" OE Statements of the form "It/mean/value/etc is above/outside/not within the CI" ⇒ BF0 Statements of the form "1.16 is above/outside/not within 96% of the data/values/weights" ⇒ BF0 Statements such as "Claim is likely/reasonable/supported/correct/true/possible/valid" ⇒ Bdep1 providing BF1 			
			10	